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## THEORETICAL AND COMPUTATIONAL APPROACH TO $(k, g)$ -SPECTRA

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For each pair of parameters  $(k, g)$ , where  $k \geq 3$  and  $g \geq 3$ , the complete set of possible orders of connected  $k$ -regular graphs with girth  $g$  is referred to as *the spectrum of orders of  $(k, g)$ -graphs*, or *the  $(k, g)$ -spectrum*. Finding the  $(k, g)$ -spectrum for a specific pair of parameters  $(k, g)$  is extremely difficult, as it requires determining the minimum order  $n(k, g)$  of the smallest connected  $k$ -regular graph with girth  $g$ . In this talk, we present some theoretical results on determining  $(k, g)$ -spectra together with some algorithms for generating  $(k, g)$ -spectra. For some specific parameter pairs, we explicitly list the  $(k, g)$ -spectra that we have determined and the associated algorithms.

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