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## DISTANCE MAGIC TYPES OF LABELINGS

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Let  $G = (V, E)$  be a graph of order  $n$ . A *distance magic labeling* of  $G$  is a bijection  $\ell: V \rightarrow \{1, 2, \dots, n\}$  for which there exists a positive integer  $\mu$  such that  $\sum_{x \in N(v)} \ell(x) = \mu$  for all  $v \in V$ , where  $N(v)$  is the open neighborhood of  $v$ . Moreover, we also consider a closed distance magic labeling as well as a  $\Gamma$ -distance magic labeling. Namely, in a *closed distance magic labeling* we take a sum of labels in closed neighborhood instead of open neighborhood of  $v$ . Whereas a  $\Gamma$ -*distance magic labeling* of a graph  $G(V, E)$  with  $|V| = n$  is an injection  $f$  from  $V$  to an Abelian group  $\Gamma$  of order  $n$  such that the weight  $w(x) = \sum_{y \in N_G(x)} f(y)$  of every vertex  $x \in V$  is equal to the same element  $\mu \in \Gamma$ . A graph  $G$  is called a *group distance magic graph* if there exists a  $\Gamma$ -distance magic labeling for every Abelian group  $\Gamma$  of order  $|V(G)|$ . The recent results in the topics will be presented in the talk.